

Macroscopic and microscopic properties of magnetically frustrated $Tb_2Ti_2O_7$

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Matériaux et Interaction en COmpétition
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Outline

Introduction

Geometrical magnetic frustration

The puzzle of $\text{Tb}_2\text{Ti}_2\text{O}_7$

Experimental results

Sample preparation and characterization

Nature of the lowest crystal field levels from entropy variation

Spin dynamics

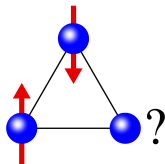
Conclusion and Outlook

Geometrical magnetic frustration

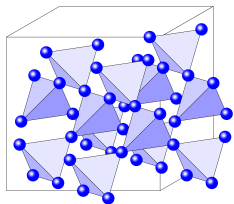
It arises when all pairwise interactions in a system cannot be satisfied simultaneously due to the geometry of the system

- ▶ Antiferromagnetically coupled Heisenberg spins on a pyrochlore lattice do not order down to $T = 0$
- ▶ Importance of other interactions:
 - ▶ exchange interactions with further neighbors
 - ▶ dipolar interaction
 - ▶ single ion anisotropy
 - ▶ etc

Example: spin ice state



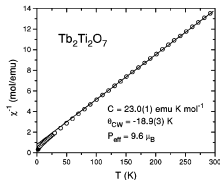
Three spins with antiferromagnetic interactions.



Pyrochlore crystal structure.

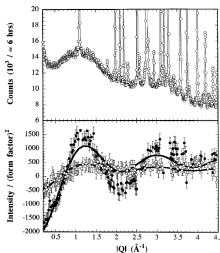
The puzzle of $\text{Tb}_2\text{Ti}_2\text{O}_7$

- ▶ Pyrochlore crystal structure
- ▶ Ising type anisotropy, but $\text{Tb}_2\text{Ti}_2\text{O}_7$ is a spin liquid, not a spin ice!
- ▶ Theory including Ising anisotropy, nearest neighbor exchange and dipolar coupling predicts order below $\simeq 1$ K
(B.C. den Hertog and M.J.P. Gingras Phys. Rev. Lett. **84** 3430 (2000))
- ▶ Even more sophisticated theories, e.g. including ground and first excited CEF states, fail to catch the essential features of $\text{Tb}_2\text{Ti}_2\text{O}_7$



No magnetic order down to
50 mK

M.J.P. Gingras *et al*, Phys. Rev. B **62** 6496 (2000)



Spin liquid correlations

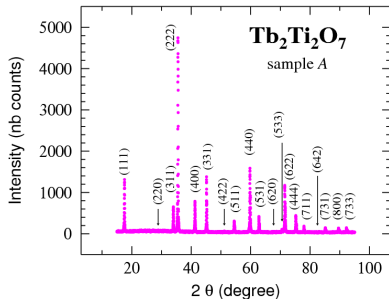


J.S. Gardner *et al*, Phys. Rev. Lett. **82** 1012 (1999)

Crystal growth of $Tb_2Ti_2O_7$

Growth conditions of different crystals

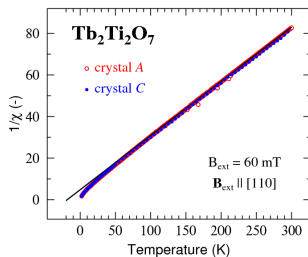
| crystals | initial powders | growth rate, flow |
|----------|-------------------|-------------------|
| <i>A</i> | $TiO_2 + Tb_4O_7$ | 8 mm/h, argon |
| <i>B</i> | $TiO_2 + Tb_4O_7$ | 8 mm/h, argon |
| <i>C</i> | $TiO_2 + Tb_2O_3$ | 7 mm/h, oxygen |
| <i>D</i> | $TiO_2 + Tb_4O_7$ | 3 & 8 mm/h, argon |



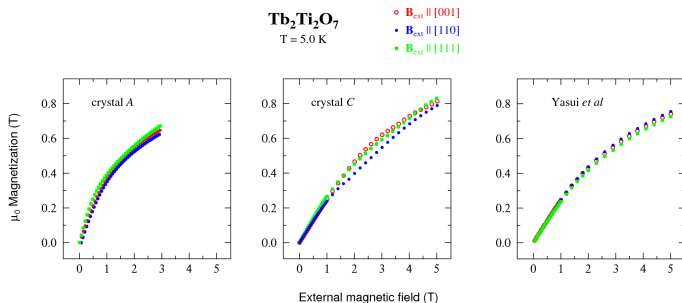
Typical x-ray powder diffraction pattern.

No foreign phase detected.

Susceptibility and magnetization of $\text{Tb}_2\text{Ti}_2\text{O}_7$

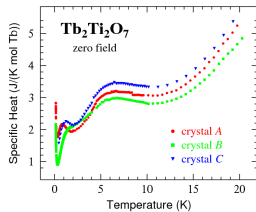


- ▶ Above 2 K, susceptibility independent of sample
- ▶ Slight differences in low temperature magnetization



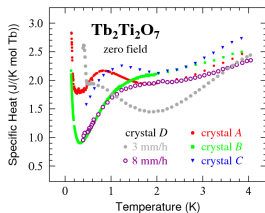
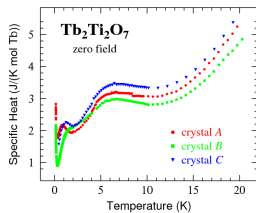
Specific heat of $Tb_2Ti_2O_7$

Our data



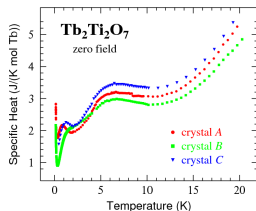
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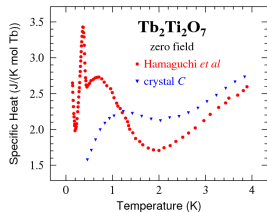
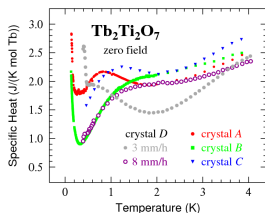
Specific heat of $\text{Tb}_2\text{Ti}_2\text{O}_7$

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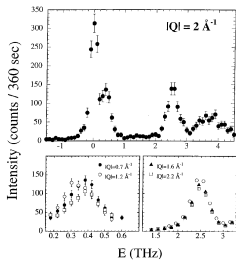


- ▶ Low temperature specific heat very sensitive to crystal growth conditions
- ▶ Transition at $\simeq 0.4$ K seems related to crystal growth velocity

Comparison with published data

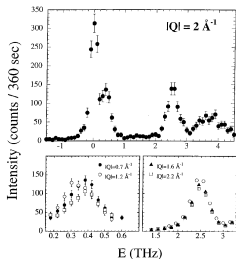


Crystal field levels of Tb^{3+} in $Tb_2Ti_2O_7$

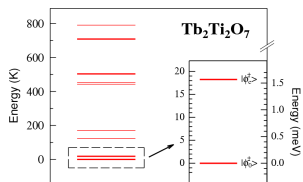


J.S. Gardner *et al*, Phys. Rev. B **64** 224416 (2001)

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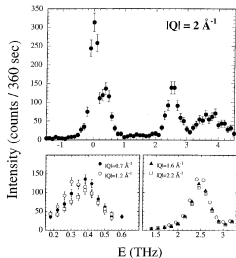


J.S. Gardner *et al*, Phys. Rev. B **64** 224416 (2001)

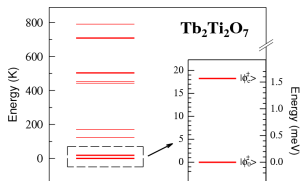


Two low-lying doublets at 0 and 18 K.

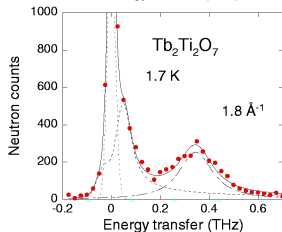
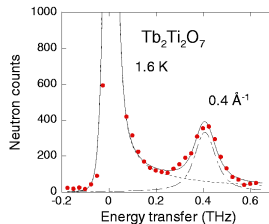
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J.S. Gardner *et al*, Phys. Rev. B **64** 224416 (2001)



Two low-lying doublets at 0 and 18 K.



I. Mirebeau *et al*, Phys. Rev. B **76** 184436 (2007)

Indication for an extra CEF level around 2 K.

Entropy variation and CEF levels

- ▶ First hypothesis: two doublets separated by an energy Δ .
 - ▶ For $T \gg \Delta$: $S = R \log 4$
 - ▶ For $T \ll \Delta$: $S = R \log 2$
 - ▶ Entropy variation:
 $\Delta S = R(\log 4 - \log 2) = R \log 2$

Entropy variation and CEF levels

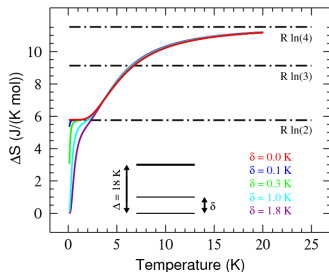
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- ▶ Second hypothesis: two singlets separated by energy δ and two other levels at higher energy $\simeq \Delta$
 - ▶ For $T \gg \Delta$: $S = R \log 4$
 - ▶ For $T \ll \delta$: $S = R \log 1 = 0$
 - ▶ Entropy variation:
 $\Delta S = R \log 4$

Entropy variation and CEF levels

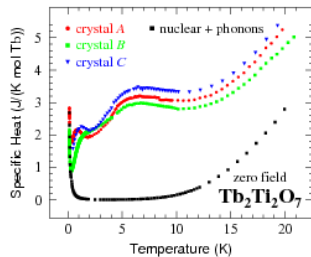
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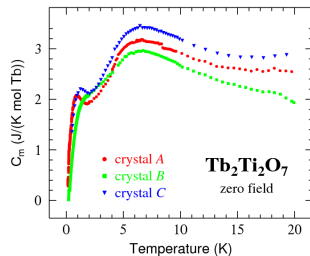
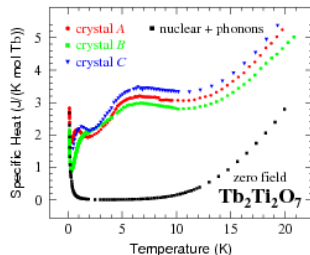


Entropy variation from
 $T = 0.13$ K to $+\infty$

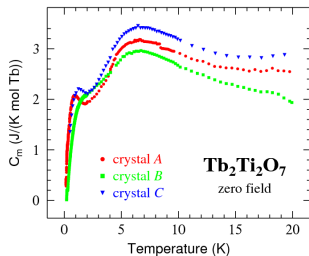
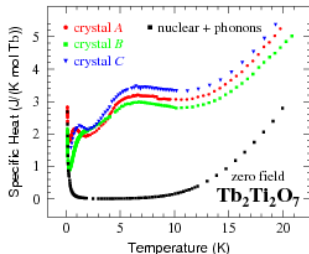
Entropy variation in $Tb_2Ti_2O_7$



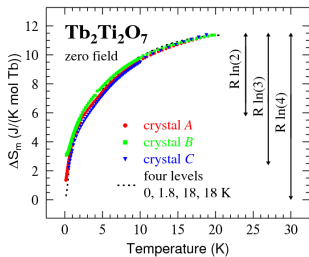
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Entropy variation in $Tb_2Ti_2O_7$



$$\Delta S(T_1 \rightarrow T_2) = \int_{T_1}^{T_2} \frac{C_m}{T} dT$$

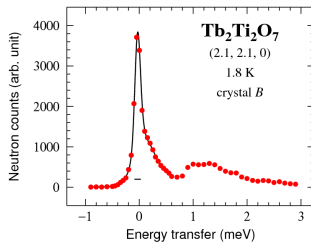
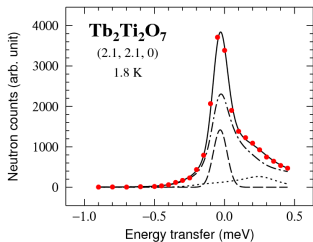


Entropy variation consistent with levels at 0, 1.8, 18 and 18 K

→ the lowest levels are two singlets

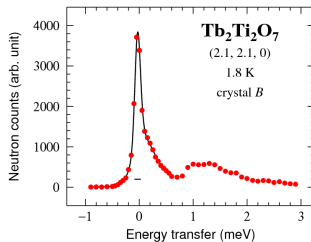
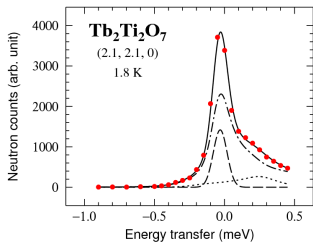
Spin dynamics in $\text{Tb}_2\text{Ti}_2\text{O}_7$

Inelastic neutron scattering experiments (IN12 at Institut Laue Langevin, Grenoble)



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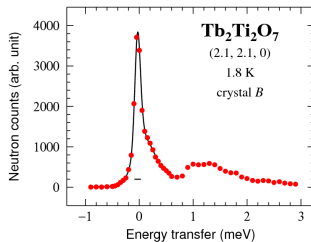
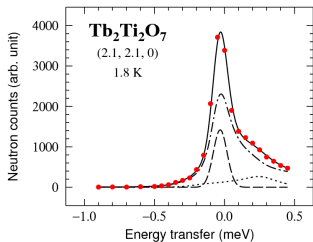


Three contributions to the low energy intensity:

- ▶ quasi-elastic scattering (Lorentzian of width Γ)
- ▶ weakly inelastic signal (CEF transition)
- ▶ incoherent scattering

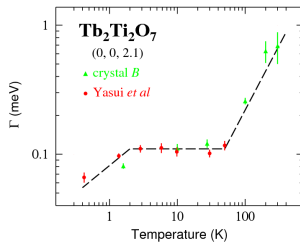
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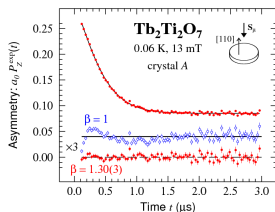
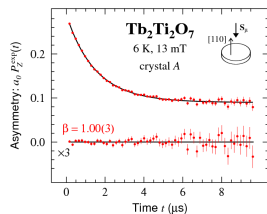
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Three temperature regimes for I 

Spin dynamics in $\text{Tb}_2\text{Ti}_2\text{O}_7$

Muon spin relaxation measurements (ISIS, UK and $S\mu\text{S}$ at PSI, Switzerland)



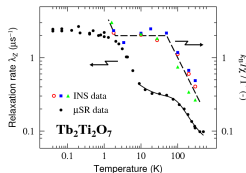
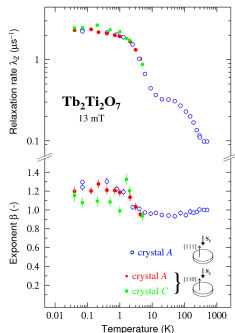
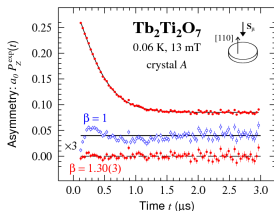
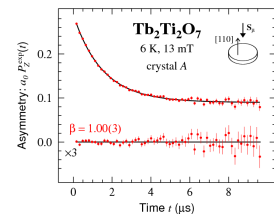
Exponential-power relaxation:

$$P_Z(t) = \exp[-(\lambda_Z t)^\beta]$$

Below $T \simeq 2$ K, $\beta > 1$

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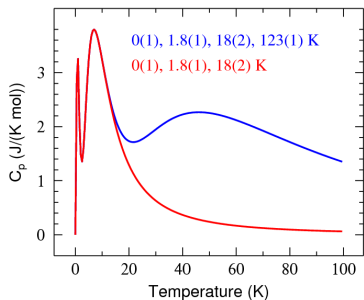
Conclusion and Outlook

- ▶ Issues in sample preparation
- ▶ Specific heat is a sensitive probe
- ▶ Entropy variation: two singlets as lower energy CEF levels
- ▶ Two characteristic temperatures in the spin dynamics
 - ▶ above 50 K: relaxation through high energy CEF levels
 - ▶ below 2 K: slowing down of Tb^{3+} fluctuations

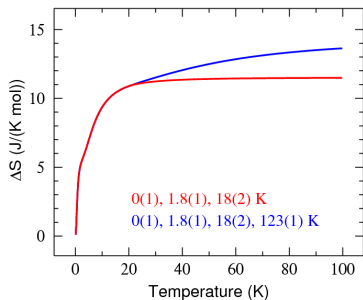
Further work

- ▶ Insight into the difference in samples
- ▶ Checking that microscopic probe results are robust
- ▶ Influence of the presence of two low-lying singlets on current models
- ▶ Why is $Tb_2Ti_2O_7$ so different from sister compound $Tb_2Sn_2O_7$?

Influence of higher energy CEF levels on entropy variation

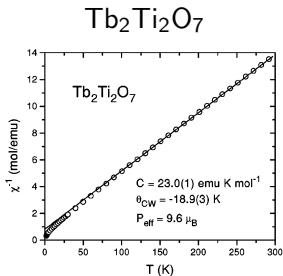


Simulated specific heat



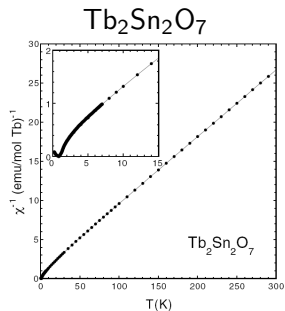
Simulated entropy variation

Susceptibility of $Tb_2M_2O_7$



No magnetic order down to
50 mK

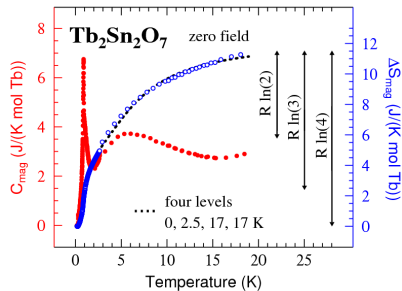
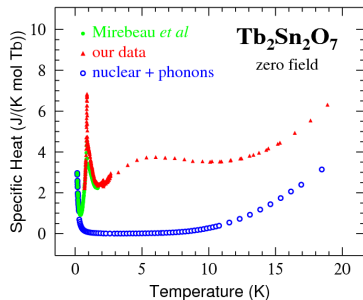
M.J.P. Gingras *et al*, Phys. Rev. B **62** 6496 (2000)



$\theta_{CW} = -13 \text{ K}$, $T_N = 0.88 \text{ K}$

K. Matsuhira *et al*, J. Phys. Soc. Japan **71** 1576 (2002)

Specific heat and entropy variation in $Tb_2Sn_2O_7$



Entropy variation consistent consistent with levels at 0, 2.5, 17 and 17 K.